

# Estimation of Statistical Power in a Multicentre MRI study.

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- 3 Voxel-Based Morphometry
- 4 Power calculation
- 5 Conclusion, References and acknowledgements.

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Statistical power definition:

- Power is the probability of rejecting the null hypothesis when it is false.

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- Pooling data from multiple centres introduces scanner related variances.
- Statistical power is bound to change depending on which region of the brain is being analyzed e.g. regions of activation in fMRI or structural differences in sMRI.
- This makes MRI power analysis rather more difficult than in a typical behavioural measure.

## Demographics:

- MRI data acquired in 2 centres (Centre I- Aberdeen , Centre II- Edinburgh).
- All patients had been diagnosed with DSM IV Unipolar major depression.
- Controls were matched based on average age, male/female ratio and estimated IQ.
- Images acquired using 1.5 T General Electric MRI scanners in both centres.

**Table:** Demographic information

Variable(Mean/SD)	Patients#I	Controls#I	Patients#II	Controls#II	Significance (P-Value)
Age (Yrs)	46.07	40.59	44.66	42.99	p=0.597
Females/Total	9/15	11/18	10/15	7/14	p=0.411
NART	111.6	114.33	115.67	117.69	p=0.566
BDI	22.93	3.15	38	1.14	p<0.001
SP	54.6	30.38	62	28.79	p<0.001
SH	35	51.36	32.13	52.71	p<0.001
Hamilton	23.2	-	27.87	-	p=0.19

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Image processing performed using SPM5.

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## Smoothing

- A Gaussian FWHM window of 8-mm used for smoothing.

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- 1 Structural differences between control/patient groups in each centre.
- 2 Scanner related differences- differences between controls from both groups.
- 3 Overall structural differences between controls and patients pooled from both centres.

# Voxel-wise Statistical Analysis

## Factorial Design:

### Design Matrix

	control I	patient I	control II	patient II
control I	1	0	0	0
patient I	0	1	0	0
control II	0	0	1	0
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### Contrasts of Interest:

- Centre I-  $[1 \ -1 \ 0 \ 0]$ , controls > patients
- Centre I-  $[-1 \ 1 \ 0 \ 0]$ , patients > controls
- Centre II-  $[0 \ 0 \ 1 \ -1]$ , controls > patients
- Centre II-  $[0 \ 0 \ -1 \ 1]$ , patients > controls

# Voxel-wise Statistical Analysis

## Factorial Design:

### Design Matrix

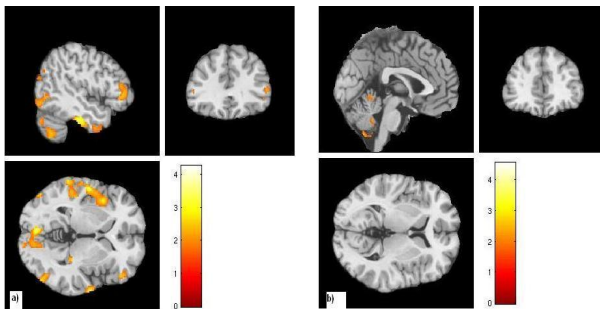
	control I	patient I	control II	patient II
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### Contrasts of Interest:

- Centre I- [1 -1 0 0], controls > patients
  - Centre I- [-1 1 0 0], patients > controls
  - Centre II-[0 0 1 -1], controls > patients
  - Centre II-[0 0 -1 1], patients > controls
- Threshold of significance:
- $p < 0.05$  corrected at a whole brain cluster level using a Monte Carlo method (Slotnick et al)

# Structural and scanner Differences-Results

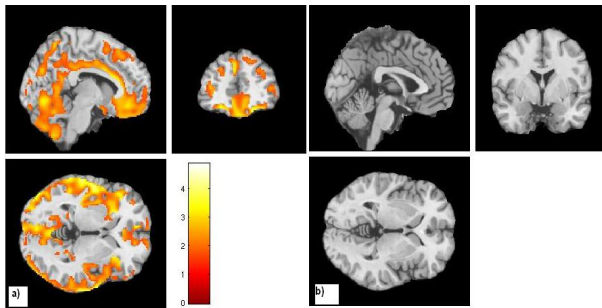
## Centre I: Controls vs Patients



**Figure:** Structural differences between patients and controls a) Patients had reduced grey matter density, b) no evidence of increase in grey matter density in the patient group.

# Structural and scanner Differences-Results

## Centre II: Controls vs Patients

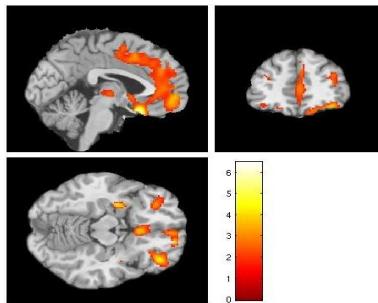


**Figure:** Structural differences between patients and controls a) Patients had reduced grey matter density, b) no evidence of increase in grey matter density in the patient group.



# Structural and scanner Differences-Results

Scanner Differences: Centre I > Centre II.



**Figure:** Scanner differences between scanner I and scanner II and whilst it might be a subject effect we think it's more likely a scanner effect.

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Factors which would influence the power outcome include:

- 1 Sample size
- 2 Effect size
- 3 Type I error e.g.  $\alpha = 0.05$ - (The odds that the observed result is due to chance)

# Data Pooling

Do Z values go up?

Table: Significant cluster peaks : Centre I subjects

Region	Brodman Area	MNI Coordinates	Z-value
Superior temporal gyrus	22	-64,-14,6	3.04
Precentral gyrus	6	-50,-2,8	2.99
Superior temporal gyrus	38	-48,8,-14	3.20
Inferior frontal gyrus	45	-50,22,14	3.08
Middle frontal gyrus	47	48,38,0	2.32

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**Table:** Significant cluster peaks: Centre II subjects

Region	Brodmann Area	MNI Coordinates	Z-value
Middle temporal gyrus	21	64,-4,-6	4.44
Inferior frontal gyrus	11	-20,28,-24	4.28
Superior temporal gyrus	38	48,12,-14	3.66
Superior temporal gyrus	38	-56,4,-6	3.84
Superior frontal gyrus	9	-8,50,34	3.94



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Do Z values go up?—Pooled data:

Table: Significant cluster peaks: Pooled data

Region	Brodman Area	MNI Coordinates	Z-value
Superior temporal gyrus	22	-58,-6,0	4.69
Middle temporal gyrus	21	64,-4,-4	4.49
Superior temporal gyrus	22	-54,0,-4	4.34
Middle Occipital gyrus	19	-50,-60,-8	4.42
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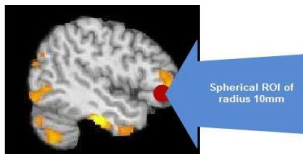
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- Clearly, by pooling Centre I and Centre II data the Z values did go up!
- Increased power is suggested by higher Z values.

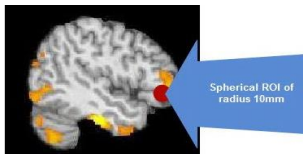
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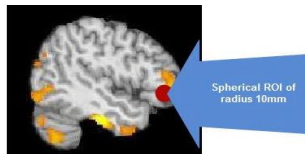
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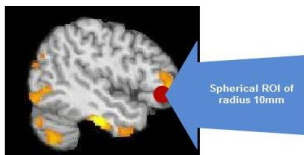
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- 1 A spherical region of interest (ROI) is selected by centering around a particular cluster point where significant structural differences were detected.
- 2 The mean representing all voxels around the ROI is computed.
- 3 Computation of effect size and study power for the contrasts of interest using Gpower 3

# Effect Size and Power Calculation

## Effect Size:

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- $N =$  total sample size (e.g. 62),  $n =$  sample size in group  $i$  (e.g. 4).

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- Offers five different types of statistical power analysis i.e. apriori, compromise, criterion, **post hoc** and sensitivity.
- Inputs to the software include: Effect size, Alpha error probability, Total sample size, numerator degrees of freedom and number of groups.

# Effect Size and Power Calculation

Power Calculation Results centre I , centre II:

Table: Power calculation results:Centre I

Region	Brodmann Area	ROI centre MNI Coordinates	Effect size	Statistical Power
Middle temporal gyrus	38	-42,4,-44	0.2725	0.5596
Insula	13	-44,14,0	0.2691	0.5393
Superior temporal gyrus	22	64,-14,6	0.3021	0.6477

Table: Power calculation results:Centre II

Region	Brodmann Area	ROI centre MNI Coordinates	Effect size	Statistical Power
Middle temporal gyrus	38	-42,4,-44	0.3435	0.758
Insula	13	-44,14,0	0.2055	0.3563
Superior temporal gyrus	22	64,-14,6	0.2938	0.6236

# Effect size and power calculation

## Power Calculation Results Pooled Data:

Table: Power calculation results:Pooled data

Region	Brodmann Area	ROI centre MNI Coordinates	Effect size	Statistical Power
Middle temporal gyrus	38	-42,4,-44	0.4348	0.9202
Insula	13	-44,14,0	0.3364	0.7404
Superior temporal gyrus	22	64,-14,6	0.4229	0.9050

As a result:

- Cohen defined effect sizes as *small*  $d=0.2$ , *medium*  $d=0.5$  and *large*  $d=0.8$ .



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- The effect sizes for all three planned ANOVA contrasts are therefore in the small to medium range.
- There is a benefit to pooling data in all regions of interest and the likelihood of rejecting the null hypothesis increases with pooled data.

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- Scanner related variances were outweighed by increase in power to detect group differences due to larger sample sizes.
- The results depend on the ROI selected.
- Efforts towards scanner harmonisation should be encouraged.
- Initial results from two of the multicentre based studies indicate that multivariate pattern recognition techniques are not largely affected by scanner related variability Kloppel., et al 2008-Alzheimer's disease study ,Mwangi, B., et al, 2010- Unipolar major depression study.

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